ABSTRACT
The IsoFilter™ technique was originally demonstrated to operate by rejecting secondary signals that derive from reflections off of a nearby metallic object – namely, the ground plane surface supporting a small pyramidal horn.[1,2] The aperture of the horn was located several wavelengths above the ground plane and the sidelobes and backlobes of the horn illuminated the ground plane itself. The success of this demonstration has been sufficient to encourage us to pursue further the question of how well the IsoFilter™ technique will work to suppress other types of secondary signals—such as signals coming from other elements of an array antenna or another individual first-order primary radiator nearby.
Here we report on some of the results of that investigation. We have calculated the far-field patterns of a sparsely populated array and applied the IsoFilter™ technique. The goodness of the suppression is judged by how well the “IsoFiltered” result agrees with the calculated pattern of the individual radiator.

Keywords: Spherical Near-Field Measurements, Near-Field Pattern Measurements, Spherical Modal Filter

1. Introduction
The usual type of SNF filtering provides for elimination of the effects of unwanted extraneous signals from the patterns produced by imperfect spherical near-field scanning, [1]. Through the use of the IsoFilter™ procedure and algorithm, the requirement that the radiating antenna of interest be located at the center of the scanning sphere can be relaxed and the filtering can be selective of a radiating antenna that is offset from the crossing point. The IsoFilter™ technique was described in a pair of postdeadline papers presented at the 2006 AMTA Symposium. [1],[2]. In those papers the two cases of measurements with an antenna offset first along the z-axis and then along a radius line were demonstrated.

The IsoFilter™ technique consists primarily of a coordinate-system translation prior to standard SNF modal filtering. While this may seem at first a minor addition of capability, it makes possible (in general) a much more selective use of the modal filtering capability inherent in SNF processing. Standard SNF filtering is always based on spheres centered on the positioner's axis intersection. The ability to translate the coordinate system permits much finer control over the sphere to be included in the processing.

This paper is primarily a discussion of intrinsic SNF modal filtering. The IsoFilter™ technique merely allows us to apply that modal filtering to any subsphere contained within the measurement sphere. As is well known, the increasingly higher modes correspond to increasing radius from the SNF coordinate origin. This allows us to grasp intuitively that reconstructing the pattern using only the lower-order modes leaves out the interference from radiators outside the sphere that corresponds to the modal order chosen.

Decades of SNF use tell us that if the radiating sources are all within a sphere, then modal content for spheres outside that will be very low. Less is known (or at least readily found in the literature) about the effects on the lower modes from significant radiation sources located outside a mode's associated radius. When trying to isolate the characteristics of an antenna (or element) from a vehicle, from other elements, or from positioner scattering, it becomes important to understand those effects. This paper is an early attempt to increase that understanding.

Here we address the fundamental issue of quantifying the degree of rejection that the IsoFilter™ technique provides. We apply the analysis to the case addressed earlier of measured data with a small pyramidal horn and to the ideal case of a simple simulated array element.

2. Quantifying the IsoFilter™ Rejection
The goal of the IsoFilter™ is to reject the influence of radiating sources that exist outside the sphere containing the sources of interest. This goal is analogous to a low-pass filter's goal of rejecting frequencies above the filter's cutoff. Just as there is no such thing as the frequently called-for
'ideal low-pass filter', we should expect some residual interference that the IsoFilter does not reject.

In this paper we take two approaches to evaluating the IsoFilter™ rejection. The first approach is to start with a small antenna at the origin, then IsoFilter™ to spheres whose centers move along the coordinate axes. Once the filtering sphere no longer contains any radiating sources, any reported signal represents interference that would add to the desired signal from an antenna located inside the filtering sphere. This approach was taken using both measured and synthesized data. The second approach is to synthesize a sparse array, then see how well we can reconstruct the pattern of the center element.

We first demonstrate an empirical procedure by which we may quantify the degree of rejection offered by the IsoFilter™ method. Recall first the configuration of the spherical near-field range on which the measurements for demonstrating IsoFilter™ were taken. It consisted of a roll-over-azimuth positioner with a fixed probe antenna. The pyramidal horn antenna was mounted above a ground plane, offset by 6 in along the roll axis. The roll and azimuth axes crossed at a point that lay precisely upon the ground plane surface. Please see Figure 1 for a photograph of the setup, where the horn is centered above the ground plane on the roll axis. The ground plane was covered by a panel of absorber to form a measurement configuration we refer to as the “bare horn” configuration, shown in Figure 2. It was demonstrated earlier[1] that the IsoFilter™ technique provided a pattern measurement result of the horn above the ground plane that agreed well with the measured pattern of the bare horn. We use that bare horn pattern data taken earlier as the basis for ascertaining a quantitative measure of the degree of rejection provided by IsoFilter™.

Figure 1 - Photograph of Spherical Near-Field Positioner for Measurement of an Antenna Above a Ground Plane

Figure 2 - Photograph of the Configuration for Measurements of the Bare Pyramidal Horn Antenna

To give a feel for the pattern of the bare horn a spherical isometric plot showing the measured forward hemisphere is provided in Figure 3.

Figure 3 - Spherical Isometric Plot of Forward Hemisphere of Bare Pyramidal Horn

After translating to the center of the aperture of the horn, the spherical modal distribution occupies modal bins that extend only up to modal order n = 5, as shown in the tabulation exhibited in Figure 4.below.

Figure 5 below illustrates the process we used to determine the IsoFilter™ rejection for the measured horn data. The IsoFilter™ sphere was translated along the X axis from 0" to 18" in 0.1" steps. For translations large enough that the horn is no longer contained in the IsoFilter™ sphere, the desired transform output should contain zero power. Any power reported in those outer spheres therefore represents imperfect IsoFilter™ rejection. If there were an AUT contained in a particular IsoFilter™ sphere, then the signal returned by this procedure represents a stray signal that would be added to the AUT signal we would be trying to isolate.

Figure 4 - Results of IsoFilter™ Rejection Measurement
Figure 4 - Summary Tabulation of Accumulated Power in Spherical Modes for Bare Horn with Origin Centered at Aperture

The sequence of translations corresponded to points along the x-axis of the measurement coordinate system, which lies in the H-plane of the horn. The data were measured at 8.0 GHz, so the 0-18" translations corresponded to approximately 0-12.2 wavelengths.

Figure 5 – Locus of Points Where IsoFilter™ Rejection Was Evaluated

Figure 6 - IsoFilter™ Rejection of Measured Horn Along x-Axis. Plot of Normalized Total Power versus Radial Distance of Filter Sphere from Center

The IsoFilter™ technique was applied over and over in steps of 0.1", and the level of the accumulated power in spherical modes corresponding to modal orders 1 through 5 was plotted as a function of translation distance. The result is shown in Figure 6.

Figure 6 above demonstrates that IsoFilter™ can provide good rejection (>35 dB) against other pattern contributors provided that the other contributors are at least 4 wavelengths distance from the radiator of interest. Note that the horn used has a physical width of about 2λ, at this frequency, and that there is significant rejection (>25 dB) as soon as the horn passes outside of the IsoFilter™ sphere (at the X-axis value of 2 in Figure 6). The use of five modes implies that the hypothetical AUT we are trying to isolate from the one horn measured can also be represented by five modes.

To investigate further the degree of rejection that IsoFilter™ might provide we next proceeded to investigate its performance using a simulated antenna.

3. Quantifying the IsoFilter™ Rejection with a Simulated Small Antenna

The second step in our investigation was to compute the rejection of IsoFilter™ for an antenna smaller than the pyramidal horn that would be formed by modeling. This was done in the interest of learning the applicability of IsoFilter™ to phased-array diagnostics. We chose one of the simplest small antennas we knew of to investigate -- namely a pair of x-polarized dipole elements separated by half a wavelength in z and formed into a little endfire array with a null at 180 degrees. With the coordinate origin half way between the elements, the spherical modal power distribution is shown in Figure 7. From this tabulation it is clear that no more than three modal orders are needed to represent the element pattern. The resulting rejection curve is shown in Figure 9.

Figure 7 - Summary Tabulation of Accumulated Power in Spherical Modes for Two-Dipole Element

Figure 8 shows one polarization component of the element's far-field pattern. This pattern plot has been rotated to an equatorial orientation to avoid polarization effects. The IsoFilter™ sphere was then translated first along x, then y, to see how much of the element's power got through the filter. The resulting rejection curves are plotted in Figure 9 and Figure 10 when the accumulated modal power levels for n= 1, 2 & 3 are used as measures of the degree of rejection.
For the cases of translation along the y- or z- axes, the rejection is significantly less, as shown by the plots in Figure 10.

4. Application of IsoFilter™ to the Case of a Simulated Array of Small Antennas

To carry the simulation of IsoFilter™ over to the case of a set of antennas, we simulated a sparsely populated array of seven elements, where each element was again a two-dipole endfire radiator. A schematic of the array is shown in Figure 11 below:

The array is sparsely populated to simulate a collection of antennas with several wavelengths of separation between each pair. There is a center element consisting of a single element and two sets of distant elements consisting of two elements and four elements respectively. Each element position is separated from its nearest neighbor by 0.5 in. At a frequency of 11.8 GHz, this separation corresponds to half a wavelength; at lower frequencies, it is less than half a wavelength. Far-field patterns were computed for this sparse array at a variety of frequencies, causing the separation to vary in terms of wavelengths. No coupling among the elements was simulated, so the far field represents the summation of several offset isolated element patterns.

Each of the seven dipole pairs in this simulation is equally weighted. This means that of the three small antennas simulated, the one in the center that we are trying to isolate has the lowest level of excitation.

A sparse array such as this can be thought of as resembling a set of broad-beam antennas and/or scatterers on a vehicle, spacecraft, or other platform.

The far field of this array exhibits rather dramatic interference among the elements. This is to be expected, since several wavelengths separate what are in effect three
subarrays. The array's far-field pattern is shown in Figure 12 below.

Figure 12 - Sparse Array's Far Field at 10.73 GHz.

The result of IsoFilter™ is exhibited by plotting the far-field pattern of the center single element after the IsoFilter™ has been applied; please see Figure 13.

Figure 13 - Center Element of Array After IsoFilter™

An overlay of the two phi cuts, before and after IsoFilter™ has been applied to the sparse array, is shown in Figure 14 below.

Figure 14 – Far Field of Sparse Array Before & After IsoFilter™ to Center Element

The comparison shows that the IsoFilter™ technique is very effective at removing the interference caused by the outer six elements. However, when one examines the comparison of the result of IsoFilter™ to the true element pattern alone, he finds some residual discrepancy as evidenced by the comparison in Figure 15:

Figure 15 – Center-Element Far Field After IsoFilter™ vs. Actual Far Field of Ideal Element

5. Comparison of IsoFilter™ to Imaging for the Simulated Array of Small Antennas

To complete our detailed investigation into the performance of IsoFilter™, we have used MI’s conventional aperture imaging software package to provide a benchmark for rejection. We take a high resolution image of a single center element available with the sparse array model corresponding to a frequency of 8.0 GHz. This is shown in Figure 16, which plots the top 30 dB of image levels over the 21 X 21 element array area - or a 10" by 10" region.

Figure 16 - Image of Single Element at 8 GHz

The visibly high sidelobe regions are distributed along the y-axis and the low sidelobe regions along the x-axis. A plot of the image level versus distance is shown in Figure 17,
comparing the fall-off in the image along the x-axis, parallel to the dipole axis, and along the y-axis, normal to the dipole axis. We noted that conventional aperture imaging had significant difficulty interpolating the portion of the dipole pattern that gets divided by $\cos(\theta)$, which of course goes to zero at the boundary of real space. The $\cos(\theta)$ term was artificially limited to 0.5 in order to get usable values in this analysis. This artificial tapering of the plane-wave spectrum may have reduced the side lobes shown in Figure 17.

We find that the IsoFilter™ technique when applied to separation of a source of radiation in a planar aperture has close-in resolution comparable to standard aperture imaging. However, the rejection levels at distances larger than a wavelength are better with aperture imaging. One should keep in mind that IsoFilter™ would have several key advantages as a basis for diagnostic imaging: Firstly, one is free to locate the test points of the IsoFilter™ origin arbitrarily, placing them anywhere within the volume of the original test sphere; whereas for aperture imaging one obtains the expected resolution only in the aperture plane. Secondly, the IsoFilter™ technique is intimately related to the pattern of the volume element being filtered; whereas with aperture imaging, the pattern of each pixel becomes lost in the digital processing.

6. Summary
Simulation of IsoFilter™ confirms our earlier experience demonstrating significant reduction of interference levels. We have investigated the fidelity of IsoFilter™ by forming rejection curves based upon the accumulated spherical modal power level computed as a function of the fictitious translation distance away from the known radiation source of a simple radiator. We have found the close-in resolution to be comparable to the close-in resolution from standard aperture imaging.

7. Acknowledgment
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8. References

Please find these two papers in the 2006 Austin Symposium Digest in the AMTA Paper Archives on the AMTA website under Invited Papers at http://www.amta.org/amta/Members/AMTAPaperArchives/tabid/78/Default.aspx
These two papers are also available at http://www.mi-technologies.com/literature/literature.htm